Multibeam volume acoustic backscatter imagery and reverberation measurements in the Northeastern Gulf of Mexico

Timoth C. Gallaudet
Scripps Institution of Oceanography

Christian de Moustier
University of California - San Diego

Follow this and additional works at: http://scholars.unh.edu/ccom

Part of the Oceanography and Atmospheric Sciences and Meteorology Commons

Recommended Citation
Multibeam volume acoustic backscatter imagery and reverberation measurements in the northeastern Gulf of Mexico

Timothy C. Gallaudet and Christian P. de Moustier

Marine Physical Laboratory, Scripps Institution of Oceanography, Mail Code 0205, 8602 La Jolla Shores Drive, La Jolla, California 92037-0205

(Received 4 June 2001; revised 16 November 2001; accepted 4 February 2002)

Multibeam volume acoustic backscatter imagery and reverberation measurements are derived from data collected in 200-m-deep waters in the northeastern Gulf of Mexico, with the Toroidal Volume Search Sonar (TVSS), a 68-kHz cylindrical sonar operated by the U.S. Navy’s Coastal System Station. The TVSS’s 360-degree vertical imaging plane allows simultaneous identification of multiple volume scattering sources and their discrimination from backscatter at the sea surface or the seafloor. This imaging capability is used to construct a three-dimensional representation of a pelagic fish school near the bottom. Scattering layers imaged in the mixed layer and upper thermocline are attributed to assemblages of epipelagic zooplankton. The fine scale patchiness of these scatterers is assessed with the two-dimensional variance spectra of vertical volume scattering strength images in the upper and middle water column. Mean volume reverberation levels exhibit a vertical directionality which is attributed to the volume scattering layers. Boundary echo sidelobe interference and reverberation is shown to be the major limitation in obtaining bioacoustic data with the TVSS. Because net tow and trawl samples were not collected with the acoustic data, the analysis presented is based upon comparison to previous biologic surveys in the northeastern Gulf of Mexico and reference to the bioacoustic literature. © 2002 Acoustical Society of America.

[DOI: 10.1121/1.1490597]

PACS numbers: 43.30.Ft, 43.30.Sf, 43.30.Vh [DLB]

I. INTRODUCTION

Demographic pressures, overharvesting of marine fish stocks, and pollution are threatening marine ecosystems worldwide and provide incentives to focus fisheries management and plankton research efforts on conservation measures, thus requiring comprehensive knowledge of population dynamics and habitat variability. Such knowledge may be gained through ocean volume acoustic backscatter measurements that have been used to study populations of fish and plankton since the deep scattering layer was identified by Eyring et al.

Sonar echoes from volume scatterers are usually quantified using target strength (TS), which is the ratio of the intensity scattered by an object at a reference distance of 1 m, to the incident intensity, and volume scattering strength ($S_V$), which is the target strength of a unit volume. For volume scattering from $n_V$ scatterers per unit volume each with a mean differential scattering cross section $\langle \sigma_{bs} \rangle$, $S_V$ and TS are related by

$$\text{TS} = 10 \log_{10} \left( \frac{\sigma_{bs}}{S_V} \right) = S_V - 10 \log_{10} (n_V) \quad \text{(dB)}.$$ \hspace{1cm} (1)

Typically, measurements of $S_V$ with a high frequency sonar are used to estimate abundance and/or biomass by estimating $\langle \sigma_{bs} \rangle$ from trawl or net tow samples with an appropriate scattering model, and using Eq. (1) to compute $n_V$. Such efforts are difficult because marine ecosystems contain multi-species, multi-size assemblages of organisms.

Another problem affecting these types of measurements is the spatial variability of zooplankton and fish, which may lead to large errors in abundance and biomass estimates obtained with single beam sonars. Single beam, vertically oriented echo-sounders have seen the most use in bioacoustic applications, but horizontally directed sonars have been used to characterize fish school structure, shape, and movement, as well as zooplankton distributions. Multibeam echo-sounders have been used in only a few bioacoustic studies to observe the swimming behavior of individual zooplankters, to demonstrate that vertical and lateral vessel avoidance by fish negatively bias abundance estimates derived from vertical echo-sounding sonars, and to provide more precise mapping and abundance of pelagic fish stocks in near-surface schools than can be obtained by vertical echo-sounding. The use of multibeam sonars in place of single-beam sonars for future bioacoustic surveys is warranted by their increased coverage, which can improve acoustic estimates of biomass and abundance and better characterize spatial distributions of organisms.

In this context, we present volume acoustic backscatter and reverberation measurements derived from data collected by the U.S. Navy’s Toroidal Volume Search Sonar (TVSS), a 68-kHz multibeam sonar capable of 360-degree imaging in a vertical plane perpendicular to its axis. We take advantage of...
the unique synoptic three-dimensional perspective afforded by this sonar system to explore and characterize the spatial and temporal structure of pelagic fish schools and the patchiness of epipelagic zooplankton found in the northeastern Gulf of Mexico. The data were collected during engineering tests of the TVSS conducted by the U.S. Navy’s Coastal System Station, Panama City, FL, in a 2-nm² area centered at 29°30’N, 86°30’W. This is a relatively flat area on the continental shelf, with water depths ranging from 190 to 200 m, situated roughly 65 nm southwest of Panama City, and 20 nm southeast of De Soto Canyon.

The TVSS includes separate cylindrical projector and hydrophone arrays, with the same 0.53-m diameter, mounted coaxially on a cylindrical tow body. The projector array has 32 elements equally spaced 11.25 degrees apart around the cylinder and designed to produce a “toroidal” beampattern that is meant to be omni-directional in the plane perpendicular to the cylinder’s axis (usually across-track) and 3.7 degrees wide at −3 dB in any plane containing the cylinder’s axis (usually along-track). The hydrophone array consists of 120 elements equally spaced every 3 degrees around the cylinder. In the work presented here, beamforming of the hydrophone array yielded 120 receive beams, each 4.95 degrees wide at −3 dB and spaced 3 degrees apart to cover the full 360 degrees around the array in the plane perpendicular to the array’s axis.

Using this multibeam geometry, we have adapted existing oceanic imaging techniques to construct acoustic backscatter imagery of horizontal and vertical planes in the ocean volume (Fig. 1). Only vertical imagery is presented in this study to characterize the spatial distributions of bioacoustic scatterers and to partially discriminate between desired bioacoustic signals and volume or boundary reverberation. This is not possible with conventional single- or dual-beam echo-sounders because of the temporal lags introduced by the successive transects required to cover a volume of ocean comparable to that sampled by the multibeam sonar on one track. However, multibeam echo-sounders have important limitations due to the beamforming process and our intent is to demonstrate some of the capabilities and limitations of multibeam sonars in bioacoustic applications.

We begin by describing the TVSS data and signal processing methods that help to interpret the acoustic backscatter images. Because net tow or trawl samples were not collected in parallel with the acoustic data, our interpretations of these images rely on comparison and reference to previous biologic surveys in the northeastern Gulf of Mexico, and on the general bioacoustic literature.

II. TVSS DATA
A. Data collection

The acoustic data presented here were collected on 9 November 1994 between 1026AM and 1131AM local time. The wind speed and sea state recorded at 0658AM were 6 knots (3 m/s) and 1.5, respectively. A CTD cast, taken at 0658AM approximately 100 m north of the location for run 1 (Fig. 2), revealed the presence of a 24.8 °C isothermal mixed layer extending to a depth of 49 m, a thermocline between 49 and 150 m depth, and a nearly isothermal layer above the bottom with a temperature of 15.6 °C. The surface salinity was 35.1 PSU, and the surface sound speed was 1534 m/s. Historical data indicate a relatively weak circulation in the region during fall months, which, with the light winds, suggests that the surface currents were either weak or absent.
The TVSS was towed at a depth of 78 m, approximately 735 m astern a ship moving at a nearly constant speed of 4.1 m/s. Three runs of 100 consecutive pings of acoustic backscatter data, from a 200 μs CW pulse of 68 kHz transmitted at 1 Hz recorded during the tests, are analyzed here. Towfish roll, pitch, heading, speed, and depth were sampled at 1 Hz (once per ping). Further information regarding the TVSS, the data collection, and the signal processing is described in Ref. 16.

B. Environmental context

Because we lacked the net tow and trawl data required to verify that biologic sources are responsible for scattering features seen in our data, we rely on historical and concurrent data for evidence. The abundance and distribution of pelagic fish in the Gulf of Mexico (GOM) were investigated by the US National Marine Fisheries Service (NMFS) during 15 cruises in the spring and fall seasons between 1988 and 1996. Trawling was performed only during daylight hours near the bottom, with the highest concentration of sampling stations centered approximately 10 nm northwest of the TVSS experiment site. For several species, the highest abundances were sampled at four sites within 1 nm of the TVSS experiment site. Thus, the NMFS survey encompassed the year, season, time of day, geographic location, and depth corresponding to the collection of the TVSS acoustic data.

Zooplankton species known to scatter sound near 68 kHz, such as euphausiids, have been observed in the north-eastern and central GOM as well. Hopkins’ observations in a region about 120 nm south of the TVSS experiment showed that zooplankton biomass was concentrated in the upper 50 m of the water column. Zimmerman and Biggs observed acoustic scattering due to zooplankton in warm- and cold-core eddies in the central eastern GOM during June 1995 using a 153-kHz acoustic Doppler current profiler. Also in the eastern central GOM, Hopkins et al. examined the landward distributions of zooplankton between May and June 1977, and found many oceanic species distributed across the Florida shelf. Ortner et al. investigated the vertical distributions of zooplankton during January and February 1981, and found zooplankton distributions to be closely tied to mixed layer depth. Ortner et al. reported observations of euphausiids and decapod shrimp in a region about 50 nm southeast of the TVSS experiment site.

C. Processing methods

The processing scheme that we have developed for the TVSS acoustic data is designed for conformal arrays and includes quadrature sampling, resampled amplitude shading, element-pattern compensation, and broadband beamforming on phase-compensated, overlapping subarrays with asymmetric projected element spacings. This procedure permits split aperture processing of the beamformed output, which is performed because the processed data also were used to study acoustic backscatter from the ocean boundaries, and the phase zero-crossing of the output phasor is the most accurate means to detect the arrival time of boundary reflections on the maximum response axis of the beam.

For each ping, the split aperture process is used to form a phasor $P(\theta,t)$ for a given beam direction $\theta$ and time sample t every 3 degrees for directions spanning the 360 degrees around the TVSS axis. The magnitude of $P(\theta,t)$ has units of volts$^2$, and is converted to squared echo amplitude according to

$$10 \log_{10}(\text{EL}_2^2(\theta,t)) = 10 \log_{10}(\text{EL}_2(\theta,t))$$

$$-RVR - \text{FG} - \text{DI} - \text{TVG},$$

where $RVR = -168 \text{ dB re:1 V}_\text{rms}/\mu\text{Pa}$ is the receive voltage response of each hydrophone, $\text{FG} = 29 \text{ dB}$ is the preamplifier fixed gain, $\text{DI} = 13 \text{ dB}$ is the array gain associated with the beamforming and split aperture processing, and $\text{TVG}$ is the system time-varying gain. The left side of Eq. (2) is equivalent to the plane wave reverberation level (RL) in the active sonar equation, which we use to compute volume scattering strength:

$$S_V = R\ell - \text{SL} + 2\text{TL} - 10 \log_{10} V$$

with $\text{TL} = 20 \log_{10} R + \alpha R$.

where $R$ is the range from the TVSS determined from $t$ and $\theta$ using constant gradient ray-tracing techniques, $\text{SL} = 216.8 \text{ dB re:1 μPa@1 m}$ is the calibrated TVSS source level, $\alpha = 0.024$ dB/m, and $V$ is the volume ensonified by the transmitted pulse within the receive beam.

Volume scattering strength images were constructed by first computing $S_V$ from Eqs. (2) and (3) for each beamformed sample in each ping, yielding 120 backscattering strength time series. These may be displayed together as a vertical slice of volume acoustic scattering strength in polar coordinates of angle versus time (Fig. 3). In this representation, echoes from the sea surface and seafloor appear as the high backscatter, horizontal features. Scattering from resonant microbubbles in the towfish’s wake and from bubble clouds formed by breaking ship waves are responsible for the high backscattering strength features near the sea surface. Other scattering structures are apparent upon adjusting the dynamic range of the display, and these will be discussed in Sec. III.

Volume scattering strength images in the plane parallel to the towfish’s direction of travel were formed by extracting $S_V$ data recorded over successive pings. Echo-integrated vertical volume backscattering strength images on either side of

FIG. 2. TVSS track lines for three consecutive runs. The data presented in this paper are processed from pings 100–199 in each of the three runs. In the figure, north is upward.
the towfish were constructed with a time gate $\delta t$ corresponding to a 1.4-m depth interval, and an along-track averaging interval of three pings.

**D. TVSS beam geometry**

The sampling and resolution characteristics of the backscattering strength images are determined by the acoustic geometry of each TVSS ping. The angular sample spacing between the maximum response axes of adjacent beams in Fig. 3 is $\theta_s = 3$ degrees, whereas the quadrature sampled time increment within each beam is $\tau_s = 160 \mu s$, which corresponds to a 12-cm sampling interval assuming a sound speed in seawater $c = 1500 \text{ m/s}$. With the TVSS pulse length $\tau_p = 200 \mu s$, the bandwidth $W = 0.88/\tau_p = 4.4 \text{ kHz}$ yields a nominal range resolution $\Delta R = c/2W = 17 \text{ cm}$.

The volumetric resolution in each ping is determined by the spatial dimensions of the volume ($V$) ensonified by the TVSS transmit pulse within each receive beam (Fig. 1). We compute $V$ as the ellipsoidal shell section formed from the intersection of the pulse, the transmit beam pattern, and the receive beam pattern at each sampling point:

$$V = \frac{2}{3} \pi R \sin(\theta_R/2)[R^3 - R^3] \quad (\text{m}^3),$$

(4)

where $R$ is the range from the center of the TVSS in meters, $R' = R + \Delta R$, the $-3$-dB receive beamwidth ($\theta_R$) is $4.95$ degrees, and the $-3$-dB transmit beamwidth ($\theta_T$) is $3.7$ degrees. The spatial dimensions of $V$ in the across-track, along-track, and vertical dimensions ($\Delta x_v$, $\Delta y_v$, $\Delta z_v$, Fig. 1) vary with range. The along-track dimension is the same for all beam angles $\theta$:

$$\Delta y_v = 2R' \sin(\theta_T/2).$$

(5)

However, the across-track and vertical dimensions of $V$ vary with range and $\theta_a$, which is defined in relation to $\theta$ in Fig. 1 as $\theta_a = \theta$ for $\theta = 0$ to $90$ degrees; $\theta_a = |180 - \theta|$ for $\theta = 91$ to $270$ degrees; and $\theta_a = (360 - \theta)$ for $\theta = 271$ to $359$ degrees. Thus, for volume cells in beams directed towards zenith and nadir, ($\theta_a = 0$ degrees)

$$\Delta x_v = 2R' \sin(\theta_R/2) \quad (\text{m}),$$

(6a)

and for volume cells in horizontal beams, ($\theta_a = 90$ degrees)

$$\Delta x_v = \Delta R + R (1 - \cos(\theta_R/2)) \quad (\text{m}),$$

$$\Delta z_v = 2R \sin(\theta_R/2) \quad (\text{m}),$$

(6b)

where $\Delta x_v$ exceeds the range resolution at $\theta_a = 90$ degrees, and $\Delta z_v$ exceeds $\Delta R$ at $\theta_a = 0$ degrees because of the curvature of the wavefront. For angles between the horizontal and vertical, the $x$ and $z$ dimensions of $V$ can be expressed as

$$\Delta x_v = 2R \sin(\theta_R/2) \cos \theta_a + \Delta R \sin(\theta_a + \theta_R/2),$$

$$\Delta z_v = 2R \sin(\theta_R/2) \sin \theta_a + \Delta R \cos(\theta_a - \theta_R/2)$$

(6c)

for $0 < \theta_a < 90 - \theta_R/2$.

Samples in adjacent beams overlap because $\theta_s < \theta_R/2$. The overlapping volume increases with range:

$$V_{ol} = \frac{2}{3} \pi R \sin((\theta_R - \theta_s)/2)[R'^{3} - R^{3}] \quad (\text{m}^3),$$

(7)

(adjacent beams),

whereas the percent overlapping volume is

$$VP_{ol} = \frac{\sin((\theta_R - \theta_s)/2)/\sin(\theta_R/2)}{100} \times 100\%$$

(adjacent beams),

(8)

yielding a range-independent volume overlapping percentage of $39.4\%$ between adjacent TVSS beams within the same ping. Volumes ensonified on successive pings in the same beam angle overlapped and increased with range beyond 62 m due to the towfish’s speed of $V_{towf} = 4.1 \text{ m/s}$ and $-3$-dB transmit beamwidth $\theta_T = 3.7$ degrees.

The backscatter images in this study were constructed using the sidescanning techniques described in Ref. 24, where samples of acoustic backscatter are extracted for the time and angle pairs that correspond to the desired horizontal or vertical plane (Fig. 1). Between discrete beam angles, samples are interpolated in time increments corresponding to the quadrature sampling interval $\tau_s$. Thus, the sample spacings in the images depend upon $\tau_s$, as well as $R$, $V_{towf}$, and $\theta_a$. The along-track sample spacing is the ping separation distance $\delta y_v = \Delta y_p$, whereas across-track and vertical sample spacings are

$$\delta x_v = c \tau_s/2 \sin \theta_a, \quad (\text{m}) \quad \text{for } \theta_s > \theta_R,$$

$$\delta z_v = c \tau_s/2 \cos \theta_a, \quad (\text{m}) \quad \text{for } \theta_s < 90^\circ - \theta_R.$$
E. System-related sources of error

A large source of error in our measurements was the angular variation in the transmitted beampattern. A maximum deviation of $-9$ dB from the calibrated source level existed when hydrostatic tests were performed on the TVSS a year before the data collection. We were unable to correct for these variations because the actual beampattern may have changed slightly during the year between the hydrostatic testing and the TVSS deployment.\textsuperscript{24}

The beampatterns of the 120 individual hydrophones introduced another source of error, because they were not identical, and their RVRs, FGs, and TVGs varied as much as $\pm 2$ dB from average values. To simplify the beamforming, we used an average of the calibrated hydrophone sensitivity values of $-168$ dB re:1V\textsubscript{rms}/\mu Pa, and we approximated the beampatterns of individual hydrophones with a cardioid-shaped magnitude response that closely matched that provided by the manufacturer. In the absence of hydrophone phase response data, we approximated the phase pattern for each element with a function proportional to the $\sin^2$ of the angle between the maximum response axes of the element and the subarray containing it. We used these response patterns because they successfully removed pointing errors which were observed in previous beamforming efforts with the TVSS.\textsuperscript{23}

Computer simulations, which used the TVSS transmit pattern and towfish attitude data for each run, indicated that the TVSS array beampatterns produced a maximum bias error of $-7$ dB and a maximum random error of $\pm 3.3$ dB in the TVSS data. After echo-integrating and averaging over successive pings, these values were reduced to approximately $-5$ dB for the bias error and $\pm 1$ dB for the random error.

Another important limitation of the data presented here is that boundary echoes at normal incidence ($\theta=0$ or 180 degrees, Fig. 3), received through the sidelobes of beams directed towards the volume, contaminated the volume backscatter received in their mainlobes. This problem is illustrated in the returns for a single ping (Fig. 3) and for a 97-ping average [Fig. 4(a)], where boundary echoes appear as high backscatter circular features tangent to the sea surface and seafloor.

The linear bands extending diagonally from the bottom into the volume in Fig. 4(a) also result from bottom sidelobe returns. We verified through computer simulations that their unique structure is a consequence of the uniform 3-degree spacing between the receive beams, and of the nonuniform sidelobe spacing within each receive beampattern. The simulation results appear in Fig. 4(b) as dashed lines that match closely the underlying linear bands and represent the times and angles of each volume beam with a sidelobe directed at the bottom during the time of the bottom echo arrival. Minor differences probably result from uncertainties in the towfish’s attitude.\textsuperscript{24}

This sidelobe interference is somewhat enhanced by our choice of a resampled Dolph–Chebyshev amplitude shading window designed to produce a nearly uniform sidelobe level between $-28$ and $-30$ dB for all the receive beampatterns.\textsuperscript{23} Lower sidelobe levels are achievable, but the corresponding increase in mainlobe beam width would degrade the spatial resolution in the images. Due to the strong boundary echo, sidelobe returns in the TVSS data, sidelobe cancellation methods are necessary to use data in the upward looking beams beyond slant ranges equal to the towfish’s depth ($-78$ m), and in the downward looking beams beyond slant ranges equal to the towfish’s altitude ($-115$ m).

One additional limitation of the data presented here is the void region with a radius of $\sim 40$ m around the TVSS (Figs. 3 and 4) caused by a fixed 53-ms blanking delay between transmission and the start of digitization. This was done because the TVSS deployment was conducted primarily to evaluate the sonar’s mine-detection capability between 50 and 750 m, so the void region helped to reduce the large amount of data collected by the sonar. This feature of the TVSS is not a problem for future bioacoustic applications because the time interval between transmit and receive is adjustable, so that the void region may be reduced.

III. IMAGERY RESULTS AND INTERPRETATION

A. Fish schools

Along-track images [Figs. 5(a) and (c)] were formed by using a vertical echo-sounding procedure to extract backscatter data in the down-looking beams at each along-track sampling point. Across-track sections [Figs. 5(b) and (d)] were formed by using the same procedure as that used to create Fig. 3. Based on the nearly concurrent NMFS trawl data, the prominent backscatter features centered at ($y=285$ m, $z=190$ m) in Fig. 5(a) and ($y=340$ m, $z=200$ m), in Fig.
We constructed a 3D shape representation of the school in Figs. 5(a) and (b) by processing multiple along-track (x,z) sections over successive pings. Bottom detection processing was used first to discriminate between acoustic backscatter from the seafloor and from the school. A threshold of 5 dB over the ambient scattering strength level was applied to detect samples in the school, and their corresponding (x,y,z) positions were determined using constant gradient ray tracing. The result [Fig. 6(a)] resembles a “stack” of elongated “tubes” extending across-track, with a few apparently suspended above the “stack.” These features are a consequence of the TVSS sampling and resolution characteristics that are fundamental limitations for any sonar (cf. Ref. 7). The resolution of each sample is defined by the spatial dimensions of the ensonified volume [Fig. 1(c)], which are $\Delta x_V = 9.9$ m, $\Delta y_V = 7.4$ m, and $\Delta z_V = 0.28$ m at the school’s center. Therefore, the elongated features in Fig. 6(a) are most likely returns from individual fish above the center of the school, because ensonified volumes in adjacent beams overlap by 39.4%, and beams adjacent to those directed towards large scatterers or boundaries exhibit a significant sidelobe response. Sidelobe response from the fish school appears in Figs. 6(b) as light blue samples at depths of 180–185 m, 40 m across-track on either side of center. These samples are about 5 dB above the ambient level and immediately precede the arcs corresponding to the bottom echo sidelobe response.

5(c) are attributed to schools of small pelagic fish. Together, the orthogonal image pairs in Fig. 5 characterize the size and scattering characteristics of the two fish schools (Table I). Although the images are limited by surface echo sidelobe interference and saturated samples, these artifacts were distinguished from biologic scatters by their arclike across-track structure [Figs. 5(b) and (d)]. Had we only constructed the along-track sections [Figs. 5(a) and (c)], these samples might have been incorrectly attributed to the acoustic backscatter from individual fish.

**TABLE I.** Fish school data corresponding to Figs. 5 and 6. The seafloor backscattering strength $S_B$ was computed and analyzed in Ref. 24. The target strength (TS) values are for ensonified volumes, and not individual fish.

<table>
<thead>
<tr>
<th></th>
<th>Run 1</th>
<th>Run 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum height above seafloor (m)</td>
<td>7.1</td>
<td>4.7</td>
</tr>
<tr>
<td>Maximum along-track dimension (m)</td>
<td>42</td>
<td>32</td>
</tr>
<tr>
<td>Maximum across-track dimension (m)</td>
<td>31</td>
<td>26</td>
</tr>
<tr>
<td>Maximum TS (dB)</td>
<td>$-24.3$</td>
<td>$-28.9$</td>
</tr>
<tr>
<td>Mean TS (dB)</td>
<td>$-45.5$</td>
<td>$-47.3$</td>
</tr>
<tr>
<td>Maximum $S_V$ (dB)</td>
<td>$-31.9$</td>
<td>$-40.1$</td>
</tr>
<tr>
<td>Mean $S_V$ (dB)</td>
<td>$-56.1$</td>
<td>$-59.8$</td>
</tr>
<tr>
<td>Mean $S_B$ (dB) at normal incidence</td>
<td>$-8.0$</td>
<td>$-9.7$</td>
</tr>
<tr>
<td>Standard deviation of $S_B$ (dB) at normal incidence</td>
<td>2.3</td>
<td>2.0</td>
</tr>
<tr>
<td>Normal incidence $S_B$ (dB) below fish school</td>
<td>8.1</td>
<td>9.9</td>
</tr>
</tbody>
</table>

FIG. 5. Vertical volume acoustic backscattering strength ($S_V$) images of two near bottom fish schools in run 1 [(a), (b)], and run 2 [(c), (d)]. The seafloor is the high backscatter, horizontal feature at $z = 193$ m in (a) and (b), and 202 m in (c) and (d). The horizontal feature with moderately high backscatter at 158-m depth in (a) is the sidelobe response of the sea surface echo, seen also in the individual (Fig. 3) and averaged (Fig. 4) ping data. The randomly distributed samples in (a) where $S_V > -40$ dB in the water column are signals that were saturated in the TVSS data acquisition system electronics. These appear as the thin arcs in Fig. 5(b) above and below the sea surface echo sidelobe return.

FIG. 6. Orthogonal images of two near bottom fish schools in run 1 [(a),(b)], and run 2 [(c), (d)]. The seafloor is the high backscatter, horizontal feature at $z = 193$ m in (a) and (b), and 202 m in (c) and (d). The horizontal feature with moderately high backscatter at 158-m depth in (a) is the sidelobe response of the sea surface echo, seen also in the individual (Fig. 3) and averaged (Fig. 4) ping data. The randomly distributed samples in (a) where $S_V > -40$ dB in the water column are signals that were saturated in the TVSS data acquisition system electronics. These appear as the thin arcs in Fig. 5(b) above and below the sea surface echo sidelobe return.
FIG. 6. (a) Three-dimensional representation of the fish school detected in run 1 [Figs. 5(a) and (b)]. The thin, elongated features are volume cells in adjacent, overlapping beams in which fish were detected. (b) Volumetric representation of the school after filtering the samples in and around the school with a $3 \times 3 \times 3$ moving average filter and thresholding the output 5 dB above the ambient scattering strength values.

To compensate for these artifacts and produce a shape characterization potentially more representative of the actual fish school, a $3 \times 3 \times 3$-sample moving average filter was applied to the scattering strength samples in and around the school. Filtered samples with scattering strengths greater than 5 dB above the ambient scattering strength were retained, yielding an oblong volumetric shape that extends slightly diagonally to the across-track direction [Fig. 6(b)]. The shape’s maximum length is three times its maximum width and over six times its maximum height (Table I). In this representation, the school appears to be concentrated near the bottom, which was generally flat with a mean depth of 193 m in this run. Although the thresholds and filter dimensions were subjectively chosen and the representation does not account for relative motion between the school and the TVSS, the school shape in Fig. 6(b) is generally similar to those observed for other schools of small pelagic fish near the bottom during daytime (cf. Ref. 26).

With our limited data, we have no way of identifying the species of fish responsible for the enhanced volume acoustic backscatter seen in Fig. 5. However, three species representing 73% of the total catch between 150 and 200 m in the NMFS trawls could be considered candidates: the round herring (*Etrumeus teres*), the rough scad (*Trachurus lathami*), and the Gulf butterfish (*Peprilus burti*). The latter is the least likely candidate because it does not have a swimbladder for sizes greater than 75 mm. The rough scad is a good candidate because its maximum observed length was 75.8 cm, and there was a tendency for the largest fish of most species to be found deeper than 150-m depth. Nonetheless, we favor the round herring (*E. teres*) as the most likely candidate because it was the most abundant species caught in the NMFS trawls near the TVSS experiment site and over all stations between 150- and 200-m depths, with an average catch rate of 2341/h for the entire GOM. Similar inferences were made by Nero et al. in their detailed acoustic study of schooling fish about 3 nm southwest of the TVSS experiment site with a 38-kHz echo-sounder. They concluded that *E. teres* was responsible for the features in their acoustic backscatter data because of the tendency of this species to form compact schools near the bottom during the day, and ascend to the middle of the water column and disperse at night.

The acoustic characteristics of the schools in the TVSS data are generally comparable to those expected from small pelagic fish. For example, *E. teres* lengths recorded during the NMFS survey averaged 13.2 cm ($L/\lambda = 6$ at 68 kHz) and had a maximum of 51.2 cm, corresponding respectively to mean and maximum target strengths of $-42$ and $-31$ dB according to Love’s model, or $-49.5$ and $-37.5$ dB using Foose’s empirical relation for clupeoids (herring and sprat) $(T S = 20 \log_{10} L - 71.9 \text{ dB})$. The mean and maximum target strengths of ensonified volumes within the two schools (Table I) span these model predictions, suggesting that small pelagic fish within individual volume cells are a possible source for the observed data. However, this is only conjecture because physical capture was not performed during the acoustic data collection.

The two- and three-dimensional (2D/3D) characterizations of near-bottom fish schools derived from the TVSS data demonstrate the potential advantages and limitations of multibeam sonars in fisheries acoustics. Two-dimensional characterizations of schooling, diel migration, seasonal migration, and feeding have been useful in understanding fish behavior. But, as far as we know, the economic and scientific advantages of multibeam sonars for 3D characterization of fish schools have only been suggested and not documented. Because fish distributions are heterogeneous, further 3D analyses may provide important information about the structure and composition of aggregations not available in 2D studies.
B. Volume scattering layers

We constructed two types of volume backscattering strength images from the TVSS data collected in the middle and upper water column, and both revealed distinct scattering layers in the upper thermocline and at the base of the mixed layer. The first type of these images [Fig. 7(a)] was formed by averaging 97 pings along the length of run 2 (Fig. 2). The figure also shows the sidelobe response of the surface echo for beams directed away from zenith, and the high backscatter near zenith due to resonant microbubbles in the towship’s wake.25

The second type of image consisted of vertical slices of volume acoustic backscattering strength formed along-track on each side of the TVSS by echo-integrating between 30- and 130-m depth, and then averaging in three-ping intervals along-track (Fig. 10). In the absence of net and trawl data, historical data suggest that epipelagic zooplankton, and to a lesser extent, micronekton, are the sources for the scattering layers, particularly the previously cited studies which showed that zooplankton distributions in the GOM are centered near the mixed layer depth and upper 50 m of the water column.18,21

Outside the Gulf of Mexico, the results of other acoustic studies using single-frequency sonars near 68 kHz generally support our hypothesis. Plueddemann and Pinkel30 observed the diel migration of scattering layers in the eastern North Pacific with a 67-kHz Doppler sonar, and used Johnson’s32 fluid sphere model to reason that the majority of scattering in their data was due to organisms with equivalent spherical radii 0.1 to 0.4 cm, and lengths 0.5 to 2.0 cm, which includes micronekton and large zooplankton such as decapod shrimp and euphausiids. However, their reasoning assumed that the animals were well described by the fluid sphere model because they also lacked coincident in situ data.

The 70-kHz results of Stanton et al.33 are more insightful because they collected mid-water trawl samples and compared them to their acoustic data. The peak scattering strengths in their data were 1–5 dB lower than those observed during the TVSS experiment (Table II) and were attributed to fish or large numbers of arthropods, including euphausiids and shrimp. Their scattering strength predictions were based on Love’s34 model for fish and Johnson’s32 model for arthropods and were within 5 dB of those measured acoustically. Because their scattering strengths were comparable to those measured in the scattering layers by the TVSS, it is likely that the TVSS data also were influenced by zooplankton and micronekton.

One of the largest sources of error in biomass estimates of oceanic zooplankton is their fine-scale patchiness (i.e., spatial variability on scale of 1 m to 1 km), so we examined this aspect of the scattering layers in the TVSS data. Most studies of zooplankton patchiness have relied on one-dimensional variance spectra or patch-finding methods, where “patch” is defined by some arbitrary criteria.35,36 Wiebe’s37 definition of a patch as “a concentration of individuals exceeding the central value in the data set” implies that patch sizes vary with the length scales covered by the data set, the “window” of samples over which the patch is determined, and the threshold concentration beyond which a patch is defined. Nero and Magnuson36 used two-dimensional acoustic transects of the Gulf Stream to illustrate the dependencies of patch size and internal patch characteristics on threshold values and window size. With knowledge of the water mass boundaries and characteristics in their data set, they were able to determine the thresholds and window sizes which produced patches that best represented the finescale features of interest. The limited coverage and in situ data in our experiment prevented us from using their approach without a large degree of subjectivity, so we characterized the patchiness of the scattering layer data by estimating the 2D variance spectra from the volume scattering coefficients corresponding to the six \( S_V \) images in Fig. 8 (see the Appendix).

The average 2D variance spectrum (Fig. 9) reveals the dominant scales of variability in the TVSS scattering layer data. Vertical variability is distributed over a relatively wide portion of the available range of spatial frequencies, with corresponding length scales of 8–33 m. These values are close to the scattering layer thicknesses in Figs. 7 and 8.
Horizontal variability is confined to a relatively narrow portion of the range of available spatial frequencies, with corresponding length scales of 30–100 m. These values are consistent with other upper water column observations of zooplankton patch lengths (cf. Refs. 36 and 37). The two dominant peaks in the region near the horizontal spatial frequency ($\mu$) of 0.02 m$^{-1}$ and between the vertical spatial frequencies ($\nu$) of 0.03 and 0.09 m$^{-1}$ may indicate a coupling between the vertical and horizontal variability at the dominant horizontal scale of 50 m. Greenlaw and Pearcy$^{38}$ used a 20-kHz sonar to suggest that such a phenomenon affected the distributions of mesopelagic micronekton off Oregon, but they based their hypothesis on separate one-dimensional vertical and horizontal variance spectra. The two-dimensional spectrum in Fig. 9 provides evidence for this type of coupling in the TVSS scattering layer data.

The average variance spectra for each run (Fig. 10) show that the patterns in the individual images are similar, but the magnitudes vary with mean scattering strengths. The spectral levels from imagery on the left side of the TVSS always exceed their counterparts on the right side because a hydrophone on the right side of the TVSS failed during the experiment, yielding a decreased gain on the right side of the array. The spectral levels for run 2 were half an order of magnitude lower than those for runs 1 and 3, suggesting that a larger scale of variability might exist which could not be resolved by the spectra in each run. These differences are most likely due to patches longer than 1 km because the three parallel runs were roughly 3.6 km long and spaced 200 m apart (Fig. 2), and coarse scale ($O(1–100 \text{ km})$) horizontal patchiness of zooplankton is common.$^{36,39}$

Despite the limitations of boundary echo sidelobe interference, we contend that the multibeam geometry of the TVSS provides a bioacoustic remote sensing capability superior to that of the conventional single beam echo-sounder. Because distributions of marine organisms vary in four dimensions ($x, y, z, t$), they can be sampled more completely by a multibeam sonar system that provides quasi-synoptic coverage through simultaneous horizontal and vertical soundings.

Multibeam systems such as the TVSS also are perfectly suited for the type of three-dimensional visualizations of biological scattering fields presented in Green et al.$^{40}$ Valuable qualitative and quantitative bioacoustic assessments, which have been mostly studied with single-beam systems, could be obtained from images like those in Fig. 8 with their 2D-point-kriging/3D-gridding techniques. TVSS data collected over the same track at various intervals (hours, days, weeks) could be used to characterize the 4D spatiotemporal dynamics of diel migration, interaction with dynamic features, and seasonal migration. In the future, we envision merging the multibeam geometry with a multifrequency or broadband capability to provide information regarding the 4D dynamics of species interactions and community structure that is presently unobtainable.

C. Mean volume reverberation

High-frequency acoustical scattering from zooplankton is important in non-bioacoustic applications because it can be a significant component of the total volume reverberation level. To quantify this for the TVSS experiment site, we used
Eq. (2) to compute reverberation levels (RL) in each beam angle and averaged them over all pings and samples prior to the first echo from the township’s wake. Pings which suffered from saturation at recording time were not used in computing the averages, so the number of pings used to average RL was less than 100 in each run. The average reverberation levels ($\overline{RL}$) for the three TVSS runs (Fig. 11) exhibit a similar angular dependence, with reverberation levels over 10 dB higher in the beams directed towards the sea surface than those directed towards the bottom (Table III). Comparison between the image in Fig. 8 and the plots in Fig. 11 indicates that the scattering layers between 40- and 80-m

![Fig. 8](image-url)

Fig. 8. (a)–(c) Along-track vertical sections of echo-integrated volume acoustic backscattering strength ($S_v$) from data 47 m across-track to the left and right of the towfish (respectively top and bottom image in each run). The corresponding mean ($\langle S_v \rangle$) profiles averaged over the number of usable pings ($N_p$) in each run are displayed to the right. Pings in which an excessive number of samples were saturated were removed from the images and not used in the averages to prevent upward biases in the $S_v$ values. $N_p = 98, 97,$ and 99 for runs 1, 2, and 3, respectively.
depth, directly above the TVSS are the primary cause for the vertical directionality of the mean volume reverberation levels, as well as the relative peaks near 290 and 70 degrees in each run. The smaller peaks and nulls in $RL$ correspond to peaks and nulls in the transmit beampattern.

Figure 11 directly quantifies the angular-dependent noise floor for non-bioacoustic applications of these TVSS data. The minimum value in the downlooking beams corresponds to a minimum $S_v$ measurable by the TVSS of $-75$ dB. The plots in Fig. 11 also emphasize that detection near the surface will be more difficult than near the bottom. Although we can expect similar results in many shallow water environments, the shape of $RL$ will vary with changes in scattering layer depths and thicknesses, as well as with the sonar’s depth, beampattern, source level, and receiver characteristics. This information is as important in Naval applications (target detection) as in acoustic studies of the sea surface, seafloor, air-sea interaction, and mixing processes. A potential application of the TVSS in a passive mode would be to image the ambient noise field of the sea surface to determine the spatial characteristics of breaking waves and the time variability of the sea surface wave spectrum.41

FIG. 9. The average of the six two-dimensional variance spectra of volume scattering coefficients corresponding to the images in Figs. 8(a)–(c). The Appendix describes the calculations, which included a two-dimensional Hanning window to reduce sidelobe leakage. The maximum and minimum length scales resolved are 2.8 and 50 m in the vertical, and 8 and 205 m in the horizontal.

FIG. 10. Log-log plots of (a) horizontal variance spectra averaged over all vertical spatial frequencies in the two-dimensional spectra computed from each image in Fig. 8; L and R refer to images formed 47 m to the left and right side of the TVSS, respectively; (b) vertical variance spectra averaged over all horizontal spatial frequencies; (c) average horizontal, and (d) vertical variance spectrum computed from (a) and (b), respectively.


Redistribution subject to ASA license or copyright; see http://acousticalsociety.org/content/terms. Download to IP:  132.177.229.80 On: Tue, 24 Nov 2015 14:58:44
D. Environmental sources of uncertainty

The most significant environmental source of uncertainty was the boundary echo sidelobe interference illustrated in Figs. 3 and 4. The scattering layer data (Table II) were not affected because we limited the slant range coverage of Fig. 8 to distances shorter than the first echo from the towship’s wake. Although the fish school $S_V$ and TS data (Table I) were obtained after the wake and surface echoes, analysis of the scattering strength time series in beams directed towards the fish schools showed that the upward bias in the fish school TS and $S_V$ due to surface reverberation was no greater than 0.5 dB. This was fortunate, because the fish school echoes would have been significantly biased if they were closer to the TVSS or if the TVSS were towed at a greater depth, particularly if they were received at the same time as the surface echo. This illustrates that, in any shallow water multibeam application, the extent to which the data are limited by boundary echo sidelobe interference depends on the experimental geometry. Although this problem was enhanced in our results because the TVSS operated with 360 degree ensonification in the vertical plane perpendicular to the array axis, it could be reduced if the TVSS ensonified in discrete angular sectors, each electronically scanned over several pings to cover the 360 degrees about the array’s axis.

There was some uncertainty regarding the sound speed used in this study because only one CTD cast was obtained about 100 m north of the location for run 1 (Fig. 2), approximately 4.5 h prior to the acoustic data collection. Any spatial variability in the local sound speed environment would have produced distortions in the processed imagery, hence errors in the scattering layer depth and thickness estimates (Table II), and fish school shape representation (Fig. 6). To evaluate the presence and effects of variability in the local sound speed environment, we processed seafloor bathymetry and sea surface relief maps using the sound speed profile in Fig. 7(b) and constant gradient ray-tracing methods, then compared them to known environmental data. If the sound speed profile were not representative of the local sound speed environment, uncompensated ray bending would produce errors in the echo arrival angles, causing the sea surface relief maps and bathymetry to “curl” upward or downward in a symmetric manner about the track’s centerline. Because the processed bathymetry was consistent with that previously obtained during bathymetric surveys performed by the Naval Oceanographic Office, and the relatively flat sea surface relief maps were consistent with the calm conditions observed during the experiment, we deemed sound speed errors negligible.

Conditions near the seafloor that may adversely affect the acoustic backscatter from near-bottom fish include seafloor relief, vegetation, and suspended sediment, but none was seen to influence our results. As shown in Fig. 5, the

**TABLE III. Average volume reverberation characteristics from Fig. 11, and computed over $N_p$ pings. $RL_{\text{max}}$ is the maximum over all angles $\theta$ at $\theta_{\text{max}}$, and $RL_{\text{min}}$ is the minimum at $\theta_{\text{min}}$.**

<table>
<thead>
<tr>
<th></th>
<th>Run 1</th>
<th>Run 2</th>
<th>Run 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_p$</td>
<td>98</td>
<td>97</td>
<td>99</td>
</tr>
<tr>
<td>$RL_{\text{max}}$ (dB)</td>
<td>187.3</td>
<td>180.2</td>
<td>184.9</td>
</tr>
<tr>
<td>$\theta_{\text{max}}$</td>
<td>355°</td>
<td>352°</td>
<td>64°</td>
</tr>
<tr>
<td>$RL_{\text{min}}$ (dB)</td>
<td>174.6</td>
<td>166.8</td>
<td>169.1</td>
</tr>
<tr>
<td>$\theta_{\text{min}}$</td>
<td>181°</td>
<td>157°</td>
<td>130°</td>
</tr>
<tr>
<td>$RL_{\text{max}} - RL_{\text{min}}$ (dB)</td>
<td>12.7</td>
<td>13.4</td>
<td>15.8</td>
</tr>
</tbody>
</table>

*Fig. 11. $N_p$-ping average of volume reverberation levels ($RL(\theta)$) (dB) for runs 1–3 [(a)–(c)]. $\theta=0$ and 180 degrees are respectively the towfish’s zenith and nadir, facing the towfish’s direction of travel.
seafloor in the region was relatively flat, so acoustic shadowing was not a potential source of uncertainty. Similarly, aquatic vegetation could not have been a source of ambiguity for the fish schools in Fig. 5 because the seagrasses capable of strongly scattering sound in the northeastern GOM are limited to depths shallower than 30 m.\textsuperscript{42} Finally, acoustic backscatter from suspended sediment was extremely unlikely in the TVSS data because the lifting velocities of the fine-grained sediments in the TVSS experiment region are much greater than the typical bottom currents expected over the Florida shelf in the winter,\textsuperscript{15} and because the scattering strengths expected from sediments at the site would have been much less than those in Table I (cf. Ref. 39).

In both the fish and zooplankton $S_V$ and TS measurements, uncertainties due to multiple scattering and extinction also were deemed negligible. These effects can occur in fish schools with densities of $50/m^3$ and greater,\textsuperscript{33} and may occur in dense swarms of macrozooplankton.\textsuperscript{43} The maximum $S_V$ values in the TVSS scattering layer data (Figs. 7 and 8; Table II) were not large enough to suggest that the density of scatterers was sufficiently high to produce multiple scattering or extinction. To evaluate the effects of extinction through the fish schools, we compared the mean normal incidence bottom backscattering strength over runs 1 and 2 to the instantaneous bottom backscattering strength values below the fish schools. Values below the school were less than a standard deviation from the mean values, and comparable to theoretical predictions for the silt and sand in the region,\textsuperscript{24} demonstrating that extinction was insignificant (Table I). In a similar manner, multiple scattering was ruled out by adjusting the dynamic range in Fig. 5 and analyzing the backscatter imagery under the schools (not shown). Multiple scattering returns would be evident as a “tail” below each school and “under” the bottom (e.g., Fig. 4 in Ref. 44), but such features were not found in the images.

Scattering and attenuation from resonant microbubbles are more common sources of uncertainty near the sea surface. They can be formed by breaking waves, propeller cavitation, and even zooplankton and fish.\textsuperscript{5,25} As with boundary reverberation, they can produce upward biases in TS and $S_V$ estimates when they are undetected. At the TVSS’s acoustic frequency of 68 kHz, resonant scattering comes from bubbles with radii equal to 48 $\mu$m, with a single bubble target strength of $-66$ dB. For down-looking sonars near the surface, attenuation through the bubble layer will decrease the backscattered energy. These effects were negligible in this study because we used the acoustic backscatter imagery to delineate regions where acceptable data could be taken. The vertical volume images in Fig. 7 and Ref. 25 were used to define the maximum bubble depth of the wake that we set as the maximum slant range for both the scattering layer imagery and mean volume reverberation calculations.

We also used horizontal volume imagery to distinguish near-surface bubble clouds from schooling fish. Bubble clouds were observed at 3-m depth 50–100 m to either side of the ship’s track, with mean volume scattering strengths of $-35$ dB, suggesting that they might be due to dense schools of large fish. Comparison between the near-surface horizontal imagery and other acoustic observations of ship wakes showed them to be bubble clouds generated by the township’s breaking bow waves, so they were not investigated with the other fish school data.

Ambient noise was a final source of uncertainty suggested by the similarity between the vertical directionality in mean volume reverberation levels (Fig. 11) and that observed for high-frequency ambient noise.\textsuperscript{4,46} However, for biologic, surface, and ship-generated ambient noise sources, the contributions were insignificant. Biologic sources known to generate sound around 68 kHz include several species of dolphin and porpoise, and snapping shrimp\textsuperscript{46} that are found in the Gulf of Mexico. However, acoustic backscatter from large scatterers like dolphin and porpoise were not observed in any of the volume and near-surface imagery, and snapping shrimp are not likely in water depths deeper than 60 m.\textsuperscript{46}

Because the sea state was only 1.5, surface-generated noise contributions were probably less than 30 dB re 1$\mu$Pa. Propeller cavitation, as evidenced by the dense bubble clouds in the township’s wake (Fig. 7), would have dominated the township-generated noise sources, but a review of cavitation noise data at frequencies near 68 kHz for ships with characteristics similar to the TVSS township’s\textsuperscript{47} (e.g., Fig. 10.15 in Ref. 4) suggests that the cavitation noise level during the TVSS experiment would have been 90–100 dB re 1$\mu$Pa @ 1 m, and even less at the TVSS due to spherical spreading and absorption losses. Had the TVSS operated at a lower frequency, and closer to the township, the cavitation noise levels may have been significant.

IV. SUMMARY AND CONCLUSIONS

In this study, we have used the data collected by the TVSS to demonstrate the advantages and limitations of multibeam sonars in bioacoustic applications. TVSS imagery showed that the most significant limitation was boundary echo sidelobe interference, which prevented zooplankton remote sensing in the volume near the range of the first boundary echo, and fish detection near the range of the first bottom echo. The 3D representation of a near-bottom fish school demonstrated the fundamental limitation of sonar resolution inherent in both multibeam and single beam characterizations of scattering fields. Angular variation in the transmit array beampattern also contributed to uncertainties in the TVSS data.

Despite these limitations, the TVSS still provided more coverage than that possible with a single beam sonar, and we used this advantage to characterize the 3D acoustic structure of near-bottom schooling fish and zooplankton scattering layers in a shallow water region of the northeastern Gulf of Mexico. Supporting previous studies in the region, the TVSS scattering layer imagery indicated that the vertical distribution of zooplankton is closely associated with the mixed layer depth. The TVSS geometry also provided the unique capability to characterize the vertical angular dependence of volume reverberation, shown to be affected by bioacoustic scattering layers lying above the sonar. In the future, modifications of the transmit array beampattern or ping repetition cycle, and the application of sidelobe cancellation techniques, could reduce the effects of boundary reverberation.
and increase the potential for toroidal multibeam sonars in bioacoustic remote sensing applications.

ACKNOWLEDGMENTS

This work was funded by the Office of Naval Research under ONR-NRL Contract No. N00014-96-1-G913. The authors would like to thank CAPT Tim Schnoor, USN (ONR), Sam Tooma, and Maria Kalcic (NRL) for their support; Candy Robertson and Lisa Tubridy (CSS) for information on the TVSS; and Pat Jordan (MPL) for administrative support. Chris Gledhill (NMFS) and Jason Link (NMFS) are thanked for providing the NMFS Small Pelagics Report. 17 Thanks are due to Jo Griffith (MPL) for help with the figures.

APPENDIX: TWO-DIMENSIONAL VARIANCE SPECTRUM

The two-dimensional variance spectrum in Fig. 9 is calculated from the backscattering coefficients \( s\gamma \) corresponding to each image in Fig. 8, where \( S\gamma = 10 \log_{10}(s\gamma) \). The \( s\gamma \) data for each image were first resampled vertically to 1.4-m depth intervals. Because the sidescanning procedure used to form the images resulted in nonuniform sample spacing which decreases away from normal incidence, the majority of the samples have spacing smaller than 1.4 m, so they were subsampled. A few samples near normal incidence (\( z = 78 \) m) are spaced 2.5 m apart, and were interpolated to 1.4-m spacing. The average horizontal sample spacing in each image is 4.1 m. The resulting \( M \times N \) image, denoted \( s\gamma'(m,n) \), is demeaned according to

\[
s\gamma'(m,n) = s\gamma(m,n) - (1/MN) \sum_{m=1}^{M} \sum_{n=1}^{N} s\gamma(m,n) \quad (m^{-1}).
\]

The two-dimensional discrete Fourier transform of \( s\gamma'(m,n) \) is computed as

\[
F\gamma(p,q) = (1/MN) \sum_{m=1}^{M} \sum_{n=1}^{N} s\gamma'(m,n)
\times e^{-2\pi i p(m-1)/M+q(n-1)/N},
\]

where \( p \) and \( q \) are vertical and horizontal spatial frequency indices, respectively. The variance spectrum is then

\[
V\gamma(p,q) = (1/MN) |F\gamma(p,q)|^2 \quad (m^{-2}).
\]

Thus, the variance spectrum is simply the two-dimensional power spectrum of the demeaned image. Figure 9 is the result of averaging the six spectra corresponding to Fig. 8.

The relationship between the indices \( p \) and \( q \) and their corresponding spatial frequencies \( \mu \) and \( \nu \) is

\[
\nu = (1/dz)(p-M/2)/M, \quad \mu = (1/dy)(q-N/2)/N,
\]

where \( dz \) and \( dy \) are the vertical and horizontal sampling intervals, respectively. The maximum and minimum positive resolvable spatial frequencies are given by

\[
\nu_{\text{max}} = 1/(2dz), \quad \nu_{\text{min}} = 1/(2dy),
\]

\[
\mu_{\text{max}} = 1/(2dy), \quad \mu_{\text{min}} = 1/(2dy).
\]

If the total depth and along-track distance spanned by each image in Fig. 8 are denoted \( Z \) and \( Y \), then the minimum resolvable spatial frequencies are also given by

\[
\nu_{\text{min}} = 2/Z, \quad \mu_{\text{min}} = 2/Y.
\]

Thus, for Figs. 8 and 9, \( dz = 1.4 \) m, \( dy = 4.1 \) m, \( Z = 100 \) m, and \( Y = 410 \) m, so that

\[
\nu_{\text{max}} = 0.35 \text{ m}^{-1}, \quad \mu_{\text{max}} = 0.12 \text{ m}^{-1},
\]

\[
\nu_{\text{min}} = 0.02 \text{ m}^{-1}, \quad \mu_{\text{min}} = 0.005 \text{ m}^{-1}.
\]

The total sample variance in the backscattering coefficients \( s\gamma'(m,n) \) corresponding to each image in Fig. 8 is given by

\[
1/(MN) \sum_{m=1}^{M} \sum_{n=1}^{N} |s\gamma'(m,n)|^2,
\]

which can be related to the variance spectrum by applying Parseval’s theorem generalized for the two-dimensional Fourier transform to Eq. (A2):

\[
(1/MN)^2 \sum_{p=1}^{M} \sum_{q=1}^{N} |F\gamma(p,q)|^2 = (1/MN) \sum_{m=1}^{M} \sum_{n=1}^{N} |s\gamma'(m,n)|^2.
\]

Substituting (A3) into (A9) yields

\[
(1/MN) \sum_{p=1}^{M} \sum_{q=1}^{N} V\gamma(p,q) = (1/MN) \sum_{m=1}^{M} \sum_{n=1}^{N} |s\gamma'(m,n)|^2,
\]

which shows that the average value of the variance spectrum is equal to the total sample variance in the original data.

13 M. Soria, P. Freon, and F. Gerlotti, “Analysis of vessel influence on spatial behaviour of fish schools using multi-beam sonar and conse-